Singularity formation in the energy-supercritical harmonic heat flow and wave maps

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The talk is concerned with the energy-supercritical harmonic heat flow and wave maps from \mathbb{R}^d into the *d*-sphere \mathbb{S}^d with $d \geq 7$. Under the assumption of 1-corotational symmetry, the problems reduce to the simplified equations

$$\partial_t u = \partial_r^2 u + \frac{d-1}{r} \partial_r u - \frac{(d-1)}{2r^2} \sin(2u), \tag{HF}$$

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 (WM)

I will present a two-step procedure based on a robust universal energy method and modulation techniques for constructing Type II blowup solutions to these equations with a precise description of its profiles. This talk is based on the following joint works with S. Ibrahim and T. Ghoul:

[1] S. Ibrahim, T. Ghoul and V. T. Nguyen, On the stability of type II blowup for the 1-corotational energy supercritical harmonic heat flow. *Anal. PDE*, 12(1): 113–187, 2019. [DOI].

[2] S. Ibrahim, T. Ghoul and V. T. Nguyen, Construction of type II blowup solutions for the 1-corotational energy supercritical wave maps. J. Differential Equations 265(7): 2968–3047, 2018. [DOI].